



Department of Mathematical Analysis and Probability Theory

Mathematical analysis. Part 1. Differential calculus

Syllabus

	Requisites of the Course
Level of higher education	First (bachelor's)
Field of Study	12 Informational technologies
Specialty	121 Software Engineering
Educational program	Computer Systems Software Engineering
Status of the discipline	Normative
Form of study	full-time
Year of study, semester	1st year, autumn semester
Scope of the discipline	5 credits, 150 hours (36 hours lectures, 36 hours practical, 78 hours self- study)
Semester control/ control measures	Exam / modular control work, calculation and graphic work
Class schedule	http://rozklad.kpi.ua
Language of instruction	English
Information about the course instructors	Lecturer: Asssociate professor, PhD, Iryna Ihorivna Golichenko, idubovetska@gmail.com Senior lecturer Iryna Petrivna Blazhievska,PhD, i.blazhievska@gmail.com Practical: Senior lecturer, Ph.D, Olena Oleksandrivna Vaneeva, vaneeva@gmail.com Associate Professor, Ph.D. N. Iryna Ihorivna Golichenko,
Placement of the course	idubovetska@gmail.com Assistant, Skorobagach Aunty Bohdanivna, <u>tetianaskorobohach@gmail.com</u> <u>https://campus.kpi.ua</u> https://do.ipo.kpi.ua/course/view.php?id=5959

Outline of the Course

1. Description of the educational discipline, its purpose, subject of study and results teaching

Description disciplines	In accordance to educational plan educational discipline "Mathematical analysis. Part 1" (GM 10.1) belongs to the cycle of mathematical, natural scientific training and is of dominant importance in the training of a specialist. He is necessary for successful assimilation special discipline Present credit module is based on students' knowledge acquired during study mathematics in high school. Discipline "Mathematical analysis. Part 2" is one of the fundamental general education disciplines that make up theoretical basis of training of engineers and programmers. Knowledge and skills, received a student under time study given educational disciplines, are used in further at studies many the following discipline professional preparation a specialist with basic and full highereducation At passing given disciplines students get acquainted with: with introduction in mathematical analysis, functions one variable (region definition, range of values, types and methods of assignment of functions, basic characteristics of functions, methods of research and construction of graphs, basic elementary functions and their graphs); basics of differential calculus functions of one variable (limit of a numerical sequence, limit of a function, the first and second significant limits and their consequences are equivalently infinitesimal functions and infinitely large functions, continuity, convexity of the function, asymptotes, classification points gap, tangent and normal to curve, derivative and differential functions, asymptotes graphics functions, extreme functions, rule Hospital , construction graphs functions). They are studying functions many variables.
Objectives disciplines	 the purpose educational disciplines is: formation in acquirers education logical thinking, development their intelligence and abilities; formation abilities to necessary intuition and erudition in questions application of mathematics, education of students in applied mathematicscultures; formation of abilities to independently use and study literature with mathematicians, develop flexibility thinking, creative independence and action
Educational subject disciplines	general mathematical properties and regularities. Functions one variable, foundations differential calculus functions one variable, differential calculus many variables
Competences	 The purpose of the educational discipline is to form students of the followingabilities: ability to abstract thinking, analysis and synthesis (GC01) Ability apply knowledge in practical situations (GC02) Ability to search, process and analyze information from various sources (GC06) Ability work in team Ability apply corresponding mathematical, scientific and technical methods, modern information technologies and computer software support, skills in working with computer networks, databases data and Internet resources for engineering solutions tasks ability detect, put and solve problems the ability to apply the skills acquired after learning disciplines "Mathematical analysis. Part 1", when studying in generalengineering and special disciplines; ability use methods mathematical analysis inengineering calculations;

	 The ability to bring the solution of the problem to a practically accepted one of the result - numbers, graphs, accurate qualitative conclusions from using various computing tools for this, tables and directories; The ability to analyze the results obtained, the ability to generalization, productions objectives and of choice ways her solution, possession culture of thinking.
Program results teaching	 Know and apply corresponding mathematical concept, methods domain, system and object-oriented analysis and mathematical modeling for software development(PRN05) Apply knowledge and understanding of differential calculus, algebrafor solution theoretical and applied engineering tasks Define and identify technological mathematical models objects at developers in computer environment new ones complexelectronic systems and choice optimal solution. Build graphs basic elementary functions, perform transformation graphs, by schedule functions determine trends process, which she models find the roots polynomials, decompose polynomials with valid coefficients on multipliers, carry out operations over complex numbers in algebraic, in trigonometric and exponential forms, to decompose the wrong fraction in the amount of polynomial and correct fraction; Find borders numerical sequences and borders functions, compare endlessly are small functions, explore function on continuity, classify breakpoints and construct asymptotes function graph, find derivatives and differentials of functions of one variable, know the applied content of the derivative, apply the differential to approximate calculations, apply differential calculus to research functions and buildings graphs, find borders by rule Hospital;

2. Prerequisites and post-requisites of the discipline (place in the structural-logical schemes teaching according to the corresponding educational program)

Prerequisites : Present credit module is based on knowledge students, acquired at studying the school course mathematicians

Post-requisites : Credit module "Mathematical analysis. Part 1" enters to cycle of mathematical, natural and scientific training and has a dominant value in preparation a specialist Present credit module is based on knowledge students, acquired at studies mathematicians by school course, and precedes educational discipline

"Mathematical analysis. Part 2".

	Number hours					
Name sections and topics	In total	in ago number of				
		Lectures	Practical	Self- study		
1	2	3 4 5				
Section 1. Differential	calculus fu	nctions one va	riable			
<i>Topic 1.1. Introduction to mathematical analysis</i>	32	12	10	6		
Topic 1.2. Differential calculus	36	10	14	6		

3 . Content of educational discipline

and its application				
MCW - I	6	-	2	4
Section 2. Differential ca	lculus func	tions many var	riables	
<i>Topic 2.1. Functions many variables:</i> <i>basic concepts, function limit, continuity</i>	10	5	3	3
Topic 2.2. Derivatives and differentialsfunctions many variables	10	5	3	3
<i>Topic 2.3. The extremum of the function of twovariables</i>	10	4	2	2
<i>MCW</i> -2	6	-	2	4
Calculated graphic work	10	-	-	10
Exam	30		-	30
In total hours	150	36	36	68

4. Educational materials and resource

Basic literature

1. Math in technical university: Textbook./ I.V. Alekseeva , V.O. Heidei , O.O. Dykhovychyny , L.B. Fedorova; under the editorship O.I. Klesova ; KPI named after Igor Sikorsky, - Kyiv: KPI named after Igor Sikorskyi, 2018. – Volume 1. - 496 p. http://ela.kpi.ua/handle/123456789/24338

2. Math in technical university: Textbook./ I.V. Alekseeva , V.O. Heidei , O.O. Dykhovychyny , L.B. Fedorova; under the editorship O.I. Klesova ; KPI named after Igor Sikorsky, - Kyiv: KPI named after Igor Sikorskyi, 2019. - T.2. - 504 p. https://ela.kpi.ua/handle/123456789/30396

3. Math in technical university: Textbook./ I.V. Alekseeva , V.O. Heidei , O.O. Dykhovychyny , L.B. Fedorova; under the editorship O.I. Klesova ; KPI named after Igor Sikorsky, - Kyiv: KPI named after Igor Sikorskyi, 2021. - Volume 3. - 456 p. https://ela.kpi.ua/handle/123456789/39003

4. Math in modern technical university Practicum Part 2. Differential and integral calculus of functions of one variable [Electronic resource]: study guide for students of higher educational institutions / I.V. Alekseeva , V.O. Gaidei , O. O. Dykhovychyny [and others]. – Electronic text data (1 file: 3.67 MB). – Kyiv : NTUU "KPI", 2015. - 249 p. https://ela.kpi.ua/handle/123456789/16620

5. Differential and integral calculus functions several variables Derentialequation. Practicum for students technical specialties / Compilers: AlekseevaI.V., come on V.O., Spiritual O.O., Fedorova LB, - Kyiv: KPI named after Igor Sikorsky,2016.- 188 pages. http://matan.kpi.ua/public/files/2016/%D0%9F%D1%80%D0%B0%D0%BA%D1%82%D0 %B8%D0%BA%D1%83%D0%BC%D0%92%D0%9C2-2016.pdf

Supporting literature

6. Differential and integral calculus of functions of one variable. Collection of tasks to typical calculation work for first-year students of technical faculties. / Composer: L. B. Fedorova, N. R. Konovalova, I. V. Alekseeva etc. — K.: IVC "Polytechnic", 2001.

7. Dubovik V. P. Higher mathematics / V. P. Dubovik, I. I. Yuryk. — Kyiv: Ignatex-Ukraine, 2013. — 648 p

8. Differential and integral calculus functions one variable Practicum forstudents AND course technical specialties / Compilers: Alekseeva I.V., come on V.O., CDykhovichny, L.B. Fedorova, - Kyiv: KPI named after Igor Sikorskyi, 2013.

http://matan.kpi.ua/public/files/PraktykumMA1.pdf

9. Dubovyk IN. P. Higher math. Collection tasks: teach _ manual _ / IN. P. Dubovyk, AND. AND.Yurik - K.: A.S.K., 2005. - 648 p.

10. Math in technical university : Practicum : IN 4th h /

AND. IN. Alekseeva, IN. AT. Heidei, AT. AT. Dykhovychny, L. B. Fedorova. — Kyiv : NTUU

"КРІ", 2014. — 752 р.

11. Adams R. A. Calculus : Complete course / R. A. Adams , C. Essex . — Toronto : PearsonCanada , 2010. — 1076 pp .

11. Zill D. G. Advanced engineering mathematics / D. G. Zill , W. S. Wright . — Burlington :Jones and Bartlett Learning , 2017. — 1004 pp .

13. Zill D. G. Calculus : Early transcendentes / D. G. Zill , W. S. Wright . — Sudbury : Jonesand Bartlett publishers , 2011. — 994 pp .

Information resources

Remote courses:

1. Mathematics for engineers and economists. Differential calculus of functionsone variable

Course for bachelors of technical and economic specialties. Lectures, practice, video lectures

Alekseeva, V.O. Gaidei, O.O. Dykhovychnyi, L.B. Fedorova, N.R. Konovalova, Dudko A.F.

http://moodle.ipo.kpi.ua/moodle/course/view.php?id=960

2. Math for engineers and economists Integral calculus functions one variable Course for bachelors technical and economic specialties lectures, practice, video lectures . I.V. Alekseeva , V.O. Gaidei , O.O. Dykhovychnyi , L.B. Fedorova, Konovalova N.R., Dudko A.F., Moskvychova K.K.

http://moodle.ipo.kpi.ua/moodle/course/view.php?id=1249

Educational content

5. Methodology

Lectures

No s/p	Name topics lectures and list basic questions
	(list didactic means, link on literature and task on Self-study)
1	Introduction. Mathematical shorthand: using symbols mathematicallogic for
	abbreviated recording mathematical statements Plurals and

	operations over them Numerical plural Limited numerical pluralsconcept
	exact upper and lower limits plural
	Task on Self-study: Concept functions. The main ones characteristics behavior
	functions.
	Recommended literature: [1], 1.1-1.4; [2], 5.
2	Concept numerical sequence and her borders Properties convergentsequences.
	Weierstrass theorem on the existence of a monotone limit sequence The number e
2	Recommended literature: [2], 6.2.
3	The limit of a function. Definition of the finite limit of a function at a point by
	Cauchy and by Heme. One-sided boundaries, conditions for the existence of the boundary of a function Englissity are small and englissity big functions
	Comparison N m and n v functions
	Recommended literature: [2], 6.1, 6.3.
4	The first significant border and her consequences. The second significant
	border and herconsequences. Table equivalent endlessly small functions.
	Recommended literature: [2], 6.3.
5	Continuity functions in points and on segment Definition continuityfunctions.
	The concept of breakpoints of a function and their classification. The main ones
	theorems about continuous on segment functions.
6	Recommended literature: [2], 6.4.
0	derivative functions. Definition derivative, her geometric and physical content Pules calculation derivative Derivatives basic elementary functions
	Recommended literature: [2], 7.1.
7	Methods differentiation derivative complex and inverted functions.
	Logarithmic differentiation Differentiation functions, given implicitly and
	parametrically.
	Recommended literature: [2], 7.1.
8	Differential function. Derivatives and differentials of higher orders. Concept
	differential functions and him geometric content. Properties differential and
	using in relatives calculations. Definition derivatives and differentials higher
	orders and their properties Formula Leibniz .
	Recommended merature: [2], 1.2.
0	The main ones theorems differential calculus. Theorems Farm Role. Lagrange
,	Koshi Rule Bernoulli — Hospital and him usingfor disclosure basic types
	of uncertainties.
	Recommended literature: [2], 7.3.
10	Formula Taylor . Concept polynomial Taylor and him residual member in
	form Peano . Breeding formulas McLaren for basic elementary functions.
	Using Taylor's formulas in approximations calculations.
	Recommended literature: [2], 7.4.
11	Descende functions has been the first desire time D for the second for the
11	Research functions by help the first derivative Definition monotony functions
	on segment necessary and sufficient conditions monotony and constancy functions on segment Definition extreme functions in points Necessary and and
	sufficient conditions the extremum of the functions in points
	Recommended literature: [2], 7.5.
12	Definition extreme functions in points Necessary and are sufficient
	conditionsextreme functions in points
	Recommended literature: [2], 7.5.
13	Research functions by help the second derivative Building graphics

	functions. Definition convex functions and points bend Necessary andare sufficient conditions convexity function on segment and points bend <i>Recommended literature</i> : [2], 7.5.
14	Asymptotes graphics functions and methods their finding. General scheme
	research function and construction graphics
1.7	Recommended dierature: [2], 7.5.
15	Concept functions many variables, region definition, value, partial derivatives
	The border and continuity, differentiability . Differentiation composed and
	implicit functions.
	Recommended literature: [2], 8.1, 8.2.
16	Partial differentials of functions of many variables. Full differential.
	Approximate calculations using the differential. Tangent plane and normal to
	the surface Taylor's formula . Functions of two variables
	Recommended literature: [2], 8.2, 8.4.
17	Scalar field, derivative by directly gradient.
	Recommended literature: [3], 11.1: [2], 8.4.
18	Extremum of functions of many variables . Local and
	conditionalextrema of a function of two variables.
	Recommended literature: [2], 8.5.

Practical classes

No	Name topics occupation and list basic questions			
s/p	(list didactic means, link on literature and task on Self-study)			
1	Plurals and operations with them			
	Task on Self-study: [4], pp. 77-83.			
2	The limit of the sequence . Task			
	on Self-study: [4], pp. 84-93.			
3	The border functions			
	Task on Self-study: [4], pp. 92-99.			
4	The first and friend notable borders and consequences with them			
	Task on Self-study: [4], pp. 100-106.			
5	Endlessly are small and endlessly big functions.			
	Task on Self-study: [4], pp. 100-106.			
6	Continuous functions. points gap			
	Task on Self-study: [4], pp. 107-114.			
7	MCW -1 "Introduction to mathematical analysis"			
8	derivative functions. Methods differentiation			
	Task on Self-study: [4], pp. 115-125.			
9	Differential functions and him application.			
	Task on Self-study: [4], pp. 126-130.			
10	Derivatives and differentials higher orders Rule Bernoulli — Hospital .			
	Task on Self-study: [4], pp. 131-138.			
11	Formula Taylor .			
	Task on Self-study: [4], pp. 139-143.			
12	Research functions by help the first derivative			
	Task on Self-study: [4], p. 144-149.			
13	Research functions by help the second derivative, construction graphs functions.			
	Task on Self-study: [4], pp. 150-158.			

14	MCW -2 "Differential calculus functions one variable"			
15	Functions many variables Partial derivatives, differentials			
	Task on Self-study: [5], page 45-57.			
16	Tangent plane and normal to surface			
	Task on Self-study: [5], page 58-63.			
17	Derivative in direction, gradient. Taylor's formula . The extremum of the			
	function of twovariables			
	Task on Self-study: [5], pp. 58-63.			
18	MCW -3 "Differential calculus functions many variables"			

6. Self-study

Study discipline includes the following types of self-study work:

- preparation to lectures and practical classes, implementation domestic tasks;
- implementation home control work (test task in remote courses on the platform Moodle);
- implementation calculation graphic works;
- preparation and implementation modular control works;
- preparation to exam

Control work

Modular control work consists with three parts:

- 1. MCW -1. "Introduction to mathematical analysis".
- 2. MCW -2. "Differential calculus functions one variable".
- 3. MCW -3. "Differential calculus functions many variables".

Goal modular control works – reveal level assimilation relevantmodules, counting points by credit-modular system modules.

Policy and CONTROL

7. Policy educational disciplines (educational component)

Recommended methods teaching: study main and auxiliary literature by subject lectures, solving tasks on practical classes and at performance housework

To a student is recommended lead detailed compendium lectures Important aspect quality assimilation material, working out methods and algorithms solution the main tasks of the discipline are independent work. It includes reading literature, review literature by topic preparation to classes, implementation calculation typical work, preparation to MCW and the exam.

Academic virtue

The policy and principles of academic integrity are defined in section 3 of the Code honor National technical university of Ukraine "Kyivskyi polytechnic institute named after Igor Sikorsky". More details: <u>https://kpi.ua/code</u>

Norms ethical behavior

Standards of ethical behavior of students and employees are defined in section 2 of the Code of Honor National technical university of Ukraine "Kyivskyi polytechnic institute name Igor Sikorsky". More details: <u>https://kpi.ua/code</u>

8. Types of control and rating system for evaluating learning outcomes (RSO)

Distribution educational time by species classes and tasks with disciplines according to with working curriculum

Semes	Educationa	al time	Distribution educational hours			Control activities		tivities	
tr	loans	Acad hour s	Lecture .	Practical .	Lab . do	Self- study + Ex .	MCW	CGW	semester attestation
1	5	150	36	36	-	78	2	1	ex.

Rating student with disciplines consists with points what he receives by

- 1) writing modular control works;
- 2) execution of calculation and graphic work (CGW is divided into several parts, according to topics)
- 3) answer on exams

The size of the starting scale $R_{\rm C} = 50$ points.

Size examination scales $R_{\rm E} = 50$ points

Size scales rated $R = R_{\rm S} + R_{\rm E} = 100$ points

System rating (weight) points and criteria assessment

1. Modular control work Weight

score -30.

The modular control work consists of three parts: MCW -1.

"Introduction to mathematical analysis" - gravimetric mark 10

MCW -2 "Differential calculus of functions of one variable" - weight point 10

MCW -3 "Differential calculus of functions of many variables" - weight point 10

Maximum mark 10+10+10=30.

Criterion assessment ICR : absence on control work -0 points ratingMCW (in points) is equal to the value percent its execution.

When performing < 60% of MCW, it is not

counted.2. Calculated graphic work (CGW).

Gravimetric mark – 20.

Criterion assessment CGW:

Non-fulfillment of CGW - 0 points. The CGW is implemented and protected by the parts that per the content corresponds to the modular one control work. Parts of the CGW are surrendered to writing MCW, and themselves MCW is protection

The CGW assessment (in points) is equal to the value of the percentage (from the maximum number of points 20) her implementation with taking into account result writing of the relevant ICR.

At performance Less 60% CGW she not is counted and must be revised

For untimely (later than a week) submission of CGW, no more is credited 60%.

3. Answer on the exam

Gravimetric score is 50.

Gravimetric mark each task 10.

On exams student performs written examination work ticket consists with1 theoretical question and 4 practical tasks

Criteria assessment

- "excellent": full answer on all task (not Less 90% necessary information; complete unmistakable solving tasks) 9 - 10 points;

- "good": enough full answer (not Less 75% necessary information) or isinsignificant inaccuracies 7 - 8 points;

- "satisfactorily": incomplete answer on task (not Less 60%) and is errors and certain deficiencies of 5-6 points;

- "fail": answer not responds conditions to "satisfactorily" (unsatisfactoryanswer, wrong solution method" 0-4 points

The maximum score is 10x5=50

Encouraging points are accrued

- by proper preparation to practical classes and active work on them;

- for prizes at faculty and university olympiads from higher education mathematicians

Maximum number encouraging points not exceeds 10% (5 points).

Conditions positive intermediate attestation

is "enrolled" from the first intermediate certification (week 8) to receive it should have not Less, than 50% possible points on moment carrying out calendar control is "enrolled" from the second intermediate certification (week 14) to receive it must also have on less than 50% possible points at the time of the event calendar control Redoing the positive final semester certification for the purpose of it increase not is allowed

Student is allowed to exam,

if him terminal rating not less 30 points at this he should haveenrolled modular control works and CGW (at least 60% completed). students, which in the ends educational semester have start rating $R_{\rm S} < 20$ points to exam not are allowed and should eliminate debts(add CGW, write MCW) to the first rearrangement.

Students with rating $20 \le R_c < 30$ have possibility to get points to admissions, by implementation admission control work on to the lastweeks educational semester

Table of transfer of R rating from educational disciplines

Table 1

$\boldsymbol{R} = \boldsymbol{R}_{\mathrm{C}} + \boldsymbol{R}_{\mathrm{E}}$	Traditional rating
$95 \le R \le 100$	Excellent
$85 \le R \le 94$	Very good
$75 \le R \le 84$	Good
$65 \le R \le 74$	Satisfactorily
$60 \le R \le 64$	Sufficient
$30 \le R \le 59$	Fail
$R_{\rm S} < 30$ or not performed others conditions admission to exam	Not admitted

IN case remote forms teaching in RSO are happening the following changes:

- Control activities are held remotely from application electronic mail, Telegram, Zoom and educational platforms Moodle, in particular in the form test control works
- The maximum amount of weight points control measures for semester R_s is installed on levels 50 points
- admission mark to exam *RD* is installed on levels 30 points
- Confirmation of the student's fulfillment of the requirements of current control and conditions of admission to exam must be displayed in the Electronic Campus .
- IN case not receiving a student admission ball, him is provided possibility increase the amount of points R_{I} , gained by the student during the semester, by conducting additional control measures to admission with appropriate reflection results in Electronic campus _
- of competencies provided by the educational program is determined by on the basis of ongoing control measures, as well as the student's fulfillment of conditions admission to exam respectively to approved by the RSO.
- Examination rating may be exhibited "automatic" by formula by counting starters points for 100-point scale:

$$R = 60 + \frac{40(R_I - R_D)}{R_C - R_D}$$

Translated to examination evaluations according to with table 1.

9. Additional information with disciplines (educational component)

IN case distance form of education, the organization of the educational process is carried out withapplication electronic mail, Telegram , video conferences in zoom , educational platforms Moodle .

Current CONTROL may to be held in in the form test control works in Moodle .

The working program of the academic discipline (syllabus):

Designed by Associate Professor of the Department of Mathematics Analysis and Probability

Theory, PhD, Iryna Ihorivna Golichenko

Adopted by the Department of MA and PT (protocol No. 16 dated 07/08/2022)

Approved by Methodical by the FMF council (protocol No 8 from 07/11/2022)